

$$U_2 - U_1 = W_{tr12} + Q_{12} + W_{diss12}$$

$$H_2 - H_1 = W_{tr12} + Q_{12} + W_{diss12}$$

$$W_{tr12} = - \int_1^2 p dV$$

$$W_{tr12} = \int_1^2 V dp$$

$U(T, V)$  kalorische Zustandsgleichung

$H(T, p)$  " "

$$H = U + p \cdot V$$

$T, p, U(T, V)$

$\downarrow$   
 $\downarrow$   $V$  (thermische Zustandsgl.)  
 $\downarrow$   $U(T, V)$  (kal.)  
 $\downarrow$   $H$   $\downarrow$   $V$

spezifische Größen

$u(T, v)$  bzw.  $h(T, p)$

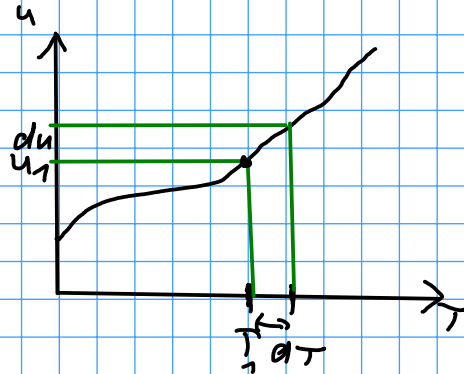
$$du = \underbrace{\left(\frac{\partial u}{\partial T}\right)_v}_{c_v} dT + \left(\frac{\partial u}{\partial v}\right)_T \cdot dv$$

$$dh = \underbrace{\left(\frac{\partial h}{\partial T}\right)_p}_{c_p} dT + \left(\frac{\partial h}{\partial p}\right)_T \cdot dp$$

$u(T)$

$$du = u'(T) dT$$

$$= \left(\frac{du}{dT}\right) \cdot dT$$



$$c_v := \left( \frac{\partial u}{\partial T} \right)_v \quad c_p := \left( \frac{\partial h}{\partial T} \right)_p \quad [c_v] = \frac{J}{kg \cdot K}$$

$c_v$  aus Wärmemessungen:

$$du = \frac{1}{m} dU = \frac{1}{m} (dQ + dW_{diss} - p dV)$$

Prozess bei konstantem Volumen, also  $dV = 0$  (isochor)

$$= \frac{1}{m} (dQ + dW_{diss})$$

$$= c_v dT$$

$$\Rightarrow \int_1^2 c_v dT = Q_{12} + W_{diss,12} \quad \left| \quad \int_1^2 c_p dT = Q_{12} + W_{diss,12} \right.$$

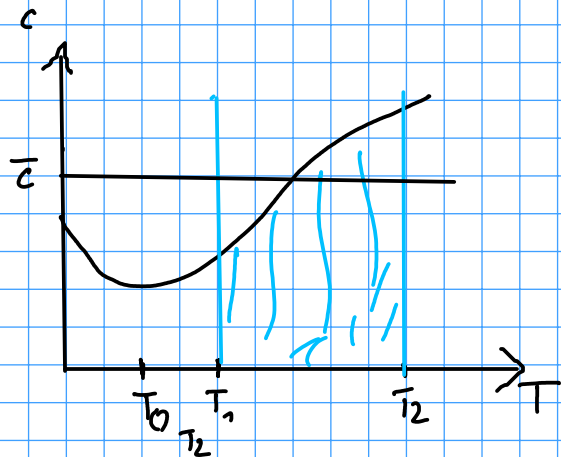
(isochor) (isobar)

speziellfall: reversibel,  $c_v$  hängt nicht von  $T$  ab  $c_p$  hängt nicht von  $T$  ab

$$m c_v \int_{T_1}^{T_2} dT = Q_{12}$$

$$m c_v (T_2 - T_1) = Q_{12}$$

$$m c_p (T_2 - T_1) = Q_{12}$$



$$\bar{c} \Big|_{T_1}^{T_2} = \frac{1}{T_2 - T_1} \int_{T_1}^{T_2} c(T) dT$$

Umkehrkal:

$$Q_{12} = m \int_{T_1}^{T_2} c(T) dT = m (T_2 - T_1) \cdot \frac{1}{T_2 - T_1} \cdot \int_{T_1}^{T_2} c(T) dT = m (T_2 - T_1) \bar{c} \Big|_{T_1}^{T_2}$$

$$Q_{12} = m \bar{c}_V \Big|_{T_1}^{T_2} (T_2 - T_1)$$

isochor + reversibel

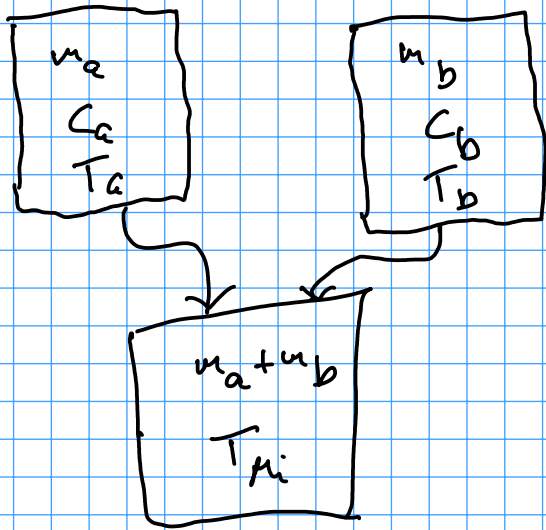
$$Q_{12} = m \bar{c}_p \Big|_{T_1}^{T_2} (T_2 - T_1)$$

isobar + reversibel

$$\int_{T_1}^{T_2} c dT = \int_{T_1}^{T_2} c dT - \int_{T_0}^{T_1} c dT$$

Tabellen für

$\bar{c}_p \Big|_{T_0}^T$ ,  $T_0 \rightarrow T$



$$Q_{b,fi} + Q_{a,fi} = 0$$

$$0 = m_b \bar{C}_b \left[ \frac{T_{fi}}{T_b} (T_{fi} - T_b) \right] + m_a \bar{C}_a \left[ \frac{T_{fi}}{T_a} (T_{fi} - T_a) \right]$$